

# General Physics II

## Basic Electric Circuits

### Resistors in Series

The Voltage “drops”:

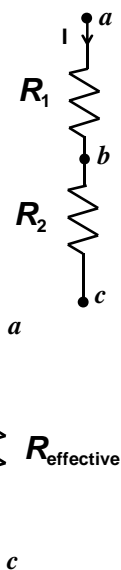
$$V_a - V_b = IR_1 \quad V_b - V_c = IR_2$$

$$V_a - V_c = I(R_1 + R_2)$$

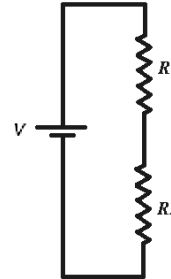
Whenever devices are in **SERIES**, the current is the same through both !

This reduces the circuit to:

Hence:  $R_{\text{effective}} = (R_1 + R_2)$



Two resistors are connected in series to a battery with voltage  $V$ . The resistances are such that  $R_1 = 2R_2$ .



Compare the current through  $R_1$  with the current through  $R_2$ :

- a)  $I_1 > I_2$       b)  $I_1 = I_2$       c)  $I_1 < I_2$

What is the potential difference across  $R_2$ ?

- a)  $V_2 = E$       b)  $V_2 = 1/2 E$       c)  $V_2 = 1/3 E$

## Resistors in Parallel

- What to do?  $V = IR$
- Very generally, devices in parallel have the same voltage drop
- But current through  $R_1$  is not  $I$ ! Call it  $I_1$ . Similarly,  $R_2 \leftrightarrow I_2$ .

$$V = I_1 R_1 \quad \text{and} \quad V = I_2 R_2$$

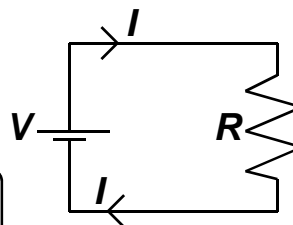
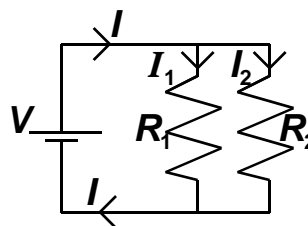
- How is  $I$  related to  $I_1$  &  $I_2$ ?

Current is conserved!

$$I = I_1 + I_2$$

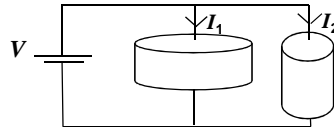
$$\Rightarrow \frac{V}{R} = \frac{V}{R_1} + \frac{V}{R_2} \Rightarrow$$

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$



Two cylindrical resistors,  $R_1$  and  $R_2$ , are made of identical material.  $R_2$  has twice the length of  $R_1$  but half the radius of  $R_1$ .

← These resistors are then connected to a battery  $V$  as shown:



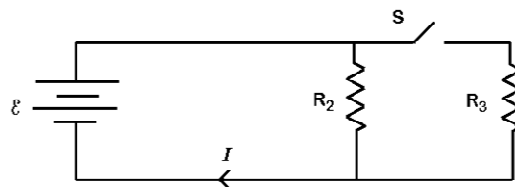
← What is the relation between  $I_1$ , the current flowing in  $R_1$ , and  $I_2$ , the current flowing in  $R_2$ ?

(a)  $I_1 < I_2$

(b)  $I_1 = I_2$

(c)  $I_1 > I_2$

Two identical light bulbs are represented by the resistors  $R_2$  and  $R_3$  ( $R_2 = R_3$ ). The switch  $S$  is initially open.



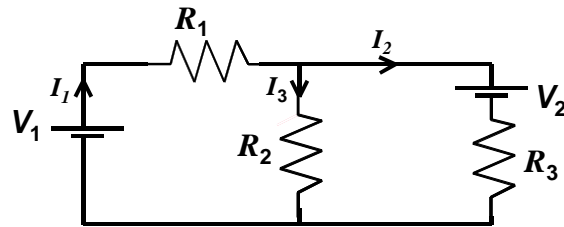
If switch  $S$  is closed, what happens to the brightness of the bulb  $R_2$ ?

- a) It increases      b) It decreases      c) It doesn't change

What happens to the current  $I$ , after the switch is closed ?

- a)  $I_{\text{after}} = 1/2 I_{\text{before}}$       b)  $I_{\text{after}} = I_{\text{before}}$       c)  $I_{\text{after}} = 2 I_{\text{before}}$

**What about circuits with non-series or parallel combinations...or more than one battery?**



### Kirchhoff's Rules

$$\sum_{loop} V_n = 0$$

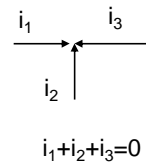
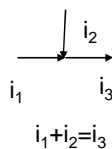
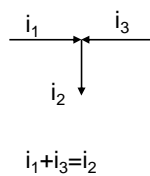
The sum of the voltages (batteries & IR combinations) around a complete loop = 0

$$I_{in} = \sum I_{out}$$

The sum of the currents at a junction = 0

### Junction Rule

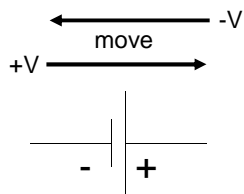
- Sum of all currents entering a junction must equal the sum of all currents leaving the junction.



$$IN = OUT$$

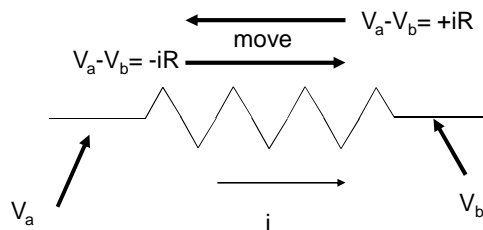
### Potential Rule for Batteries

- For a move from the negative terminal to the positive terminal then the change in potential is  $+V$   
    ← For a move from “+” to “-” then the change in potential is  $-V$

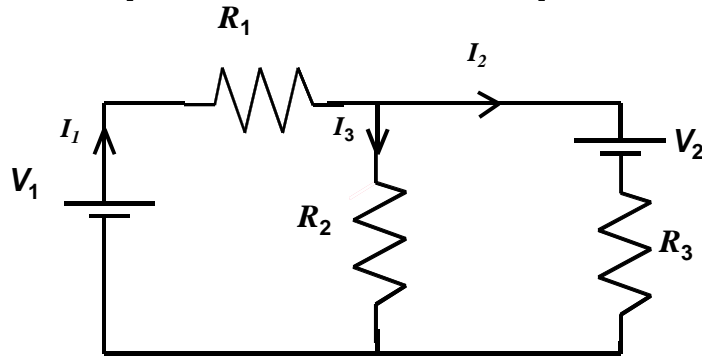


### Potential Rule for Resistors with Current

- For a move through a resistor in the direction of current, the change in potential is  $-iR$   
    ← If the move opposes the current then the change in potential is  $+iR$ .



**Let's put these ideas into practice....**



**End of  
Basic Electric  
Circuits  
Lecture**